## The Generalized Law of Demand

## TheoryGuru applications

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## Load Economicreasoning package only if it is not already loaded

```
If[Length@Names["PLTools`*"] < 10,
    Get["http://economicreasoning.com"]]
```


## Notes

$p$ and $p$ ' are each a price vector.
$q[u, p]$ is the vector of Hicksian demands corresponding to utility/output $u$.

In the Wolfram Language, x.y refers to the tensor DOT PRODUCT, NOT scalar multiplication. For TheoryGuru purposes, tensor means vector, so that the result of $x . y$ is a scalar.

## Setup

revealedpreference =

```
{p.q[u, p] \leq p.q[u, p'](* q[u,p] is cost minimizing for p *),
    p'.q[u, p'] s p'.q[u, p](* q[u,p'] is cost minimizing for p' *)};
```

This holds for any number of goods (i.e., regardless of the lengths of the vectors).
This holds even if:

- preferences are not convex,
- demand functions are not continuous,
- more than one price is changing, and
- the price changes are not marginal


## Result

$$
\begin{aligned}
& \text { TheoryGuru }[\text { revealedpreference, } \\
& \left.\left(p^{\prime}-p\right) \cdot\left(q\left[u, p^{\prime}\right]-q[u, p]\right) \leq 0\right]
\end{aligned}
$$

True

If $p$ and $p$ ' are the same except for the $i$ th price, then this result just says that the own substitution effect is negative for good $i$.

## Variable interpretations

